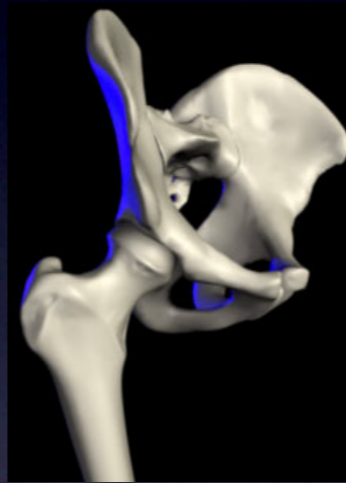


Case Study IV: Geometrical Modeling of the heart and the head

Moritz Dannhauer

Motivation

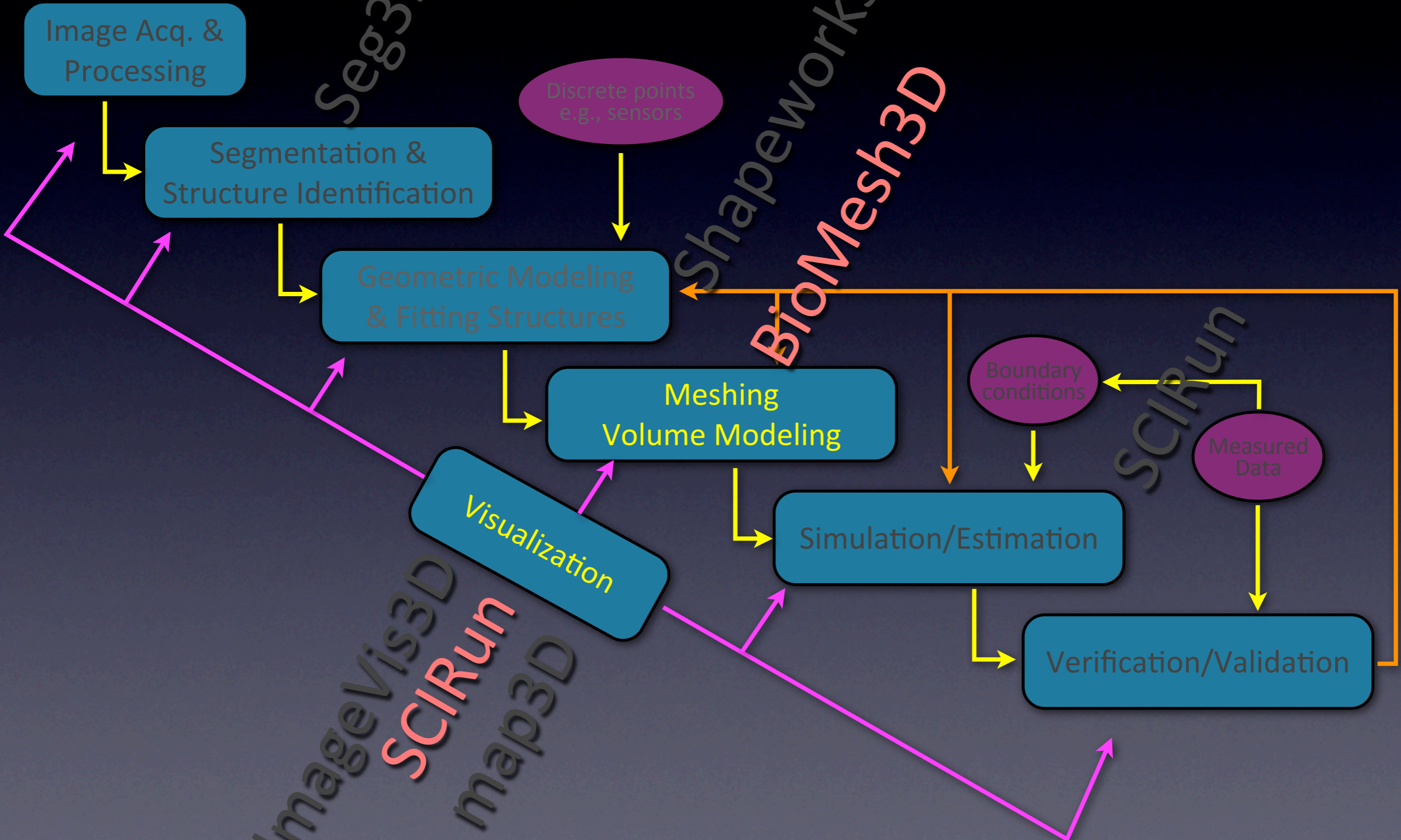
- Geometrical modeling for simulation



Content

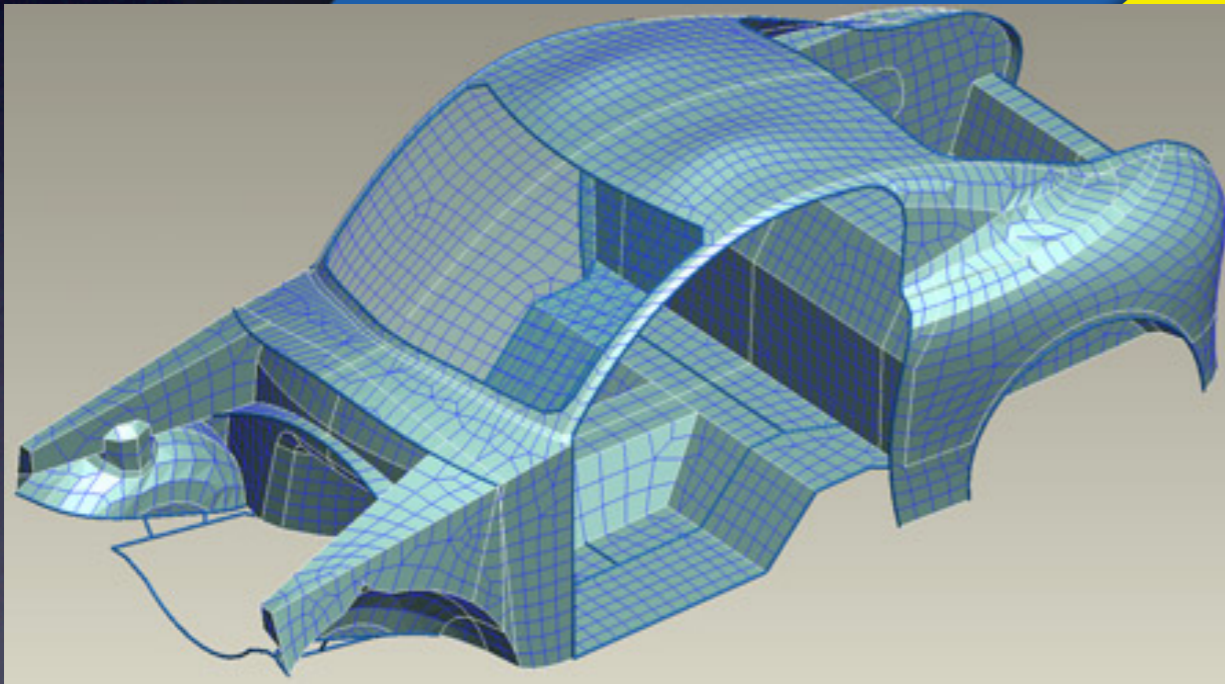
- Meshing
- BioMesh3D
- new Meshing Approach: Cleaver

Pipeline



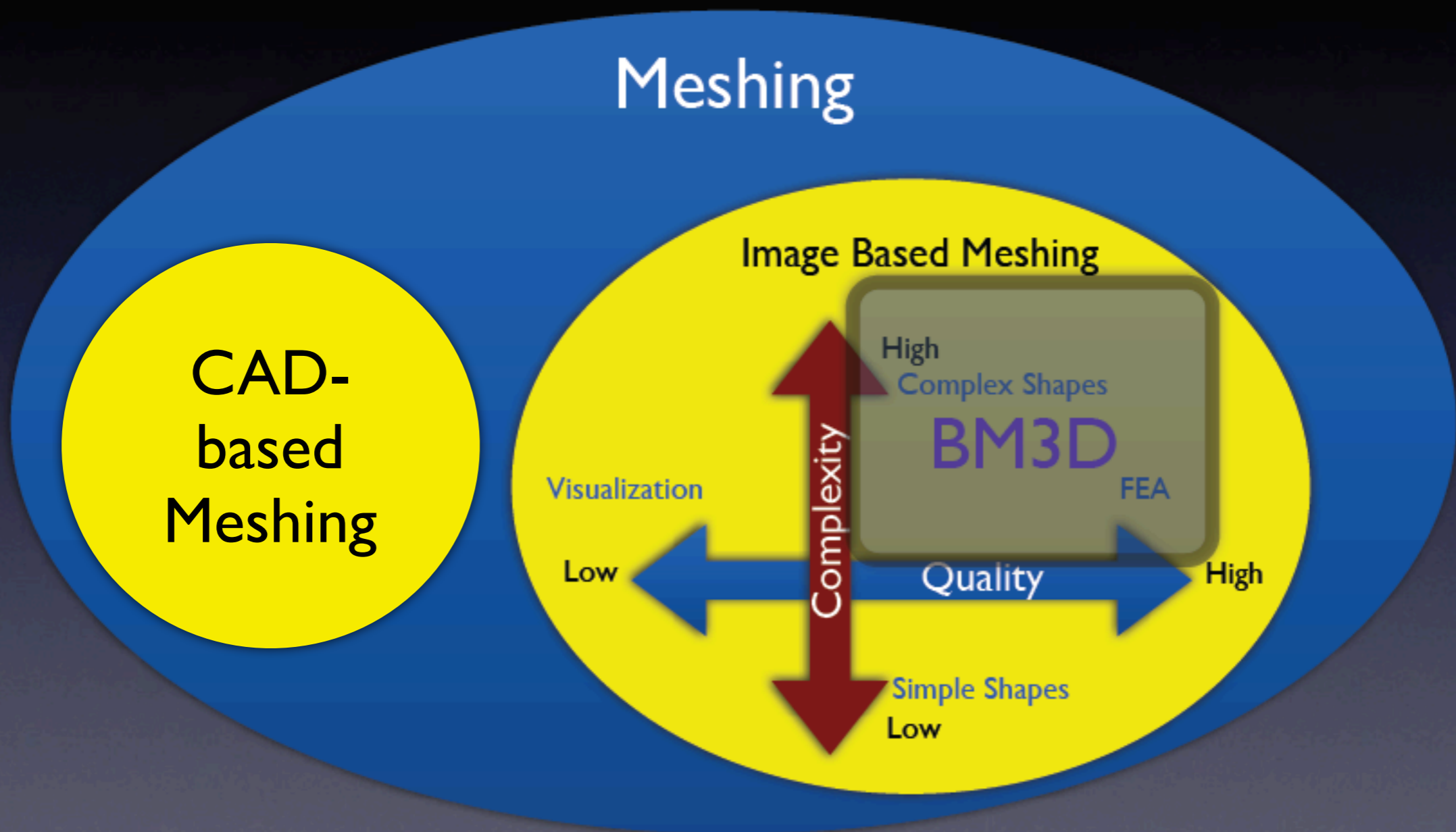
Meshing

Meshing



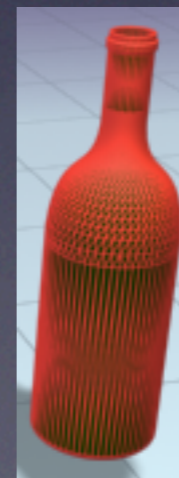
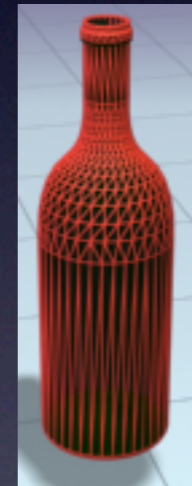
CAD-based
Meshing

Meshing



Three Scenarios

- Low detail models
- Medium detail models
- High detail models

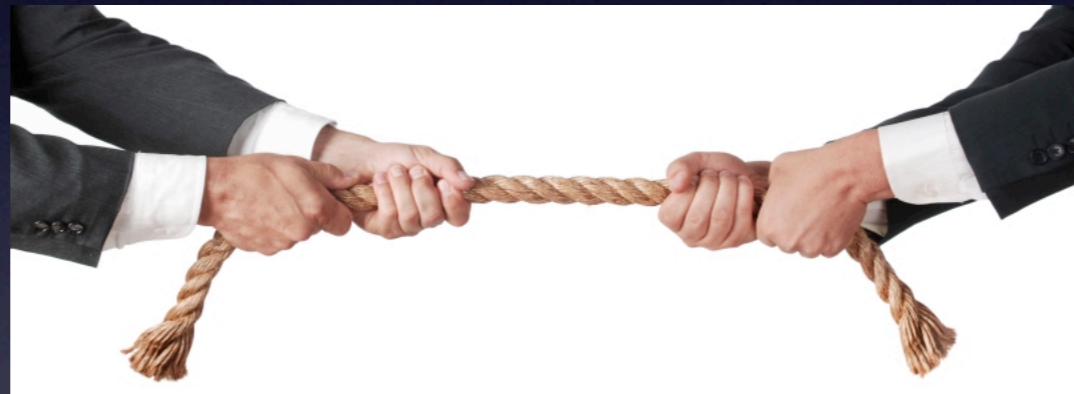


Challenges of Meshing

irregular features

multi-material

adaptive mesh



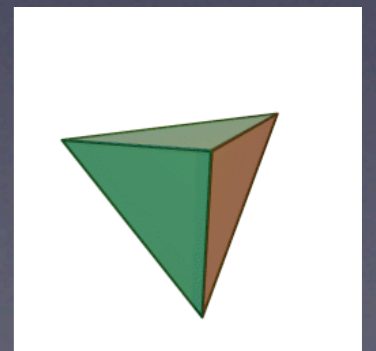
run time

small meshes

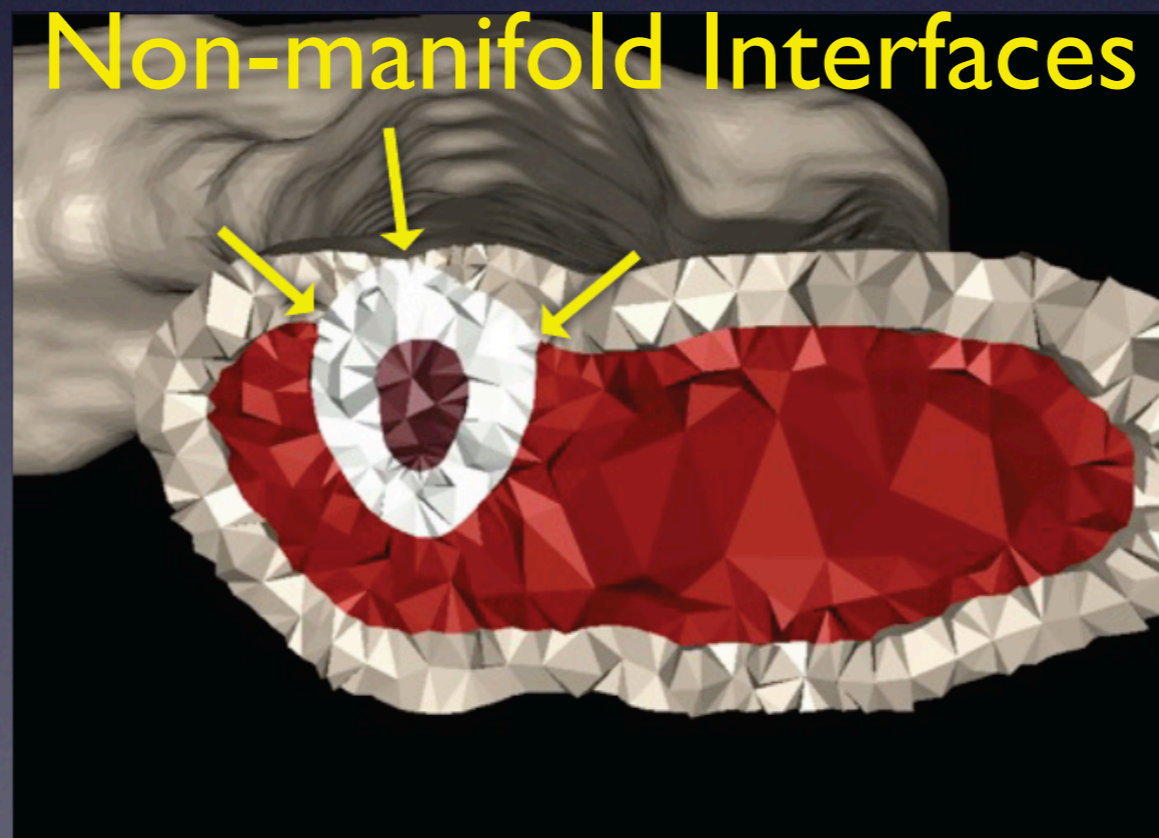
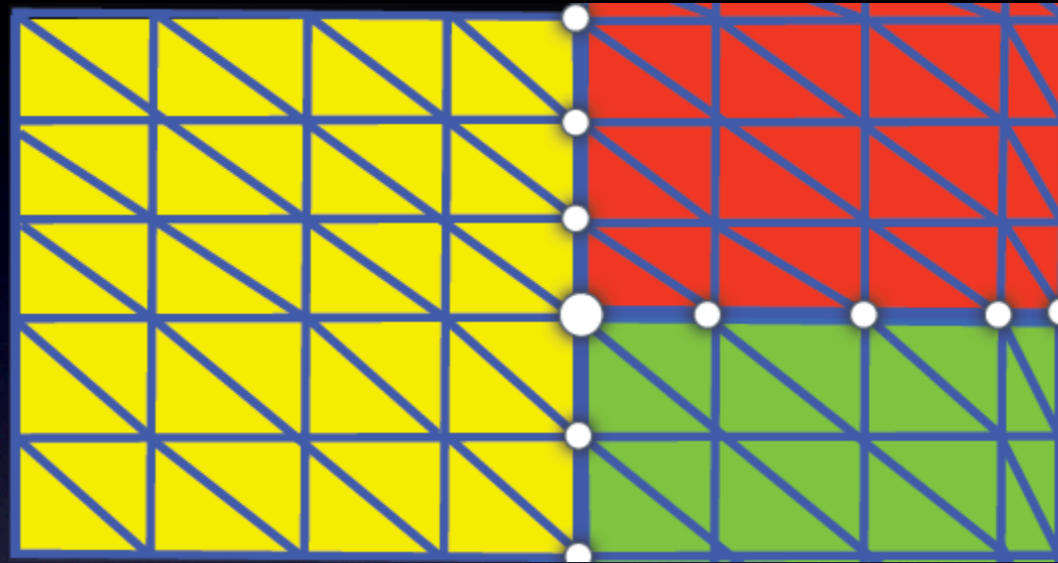
etc.

What is BioMesh3D?

- Tetrahedral conforming volume meshing
- Adaptive, multi material, subvoxel accuracy
- Goal: Determine accurate boundary surfaces
- Tetrahedralization (external): TetGen

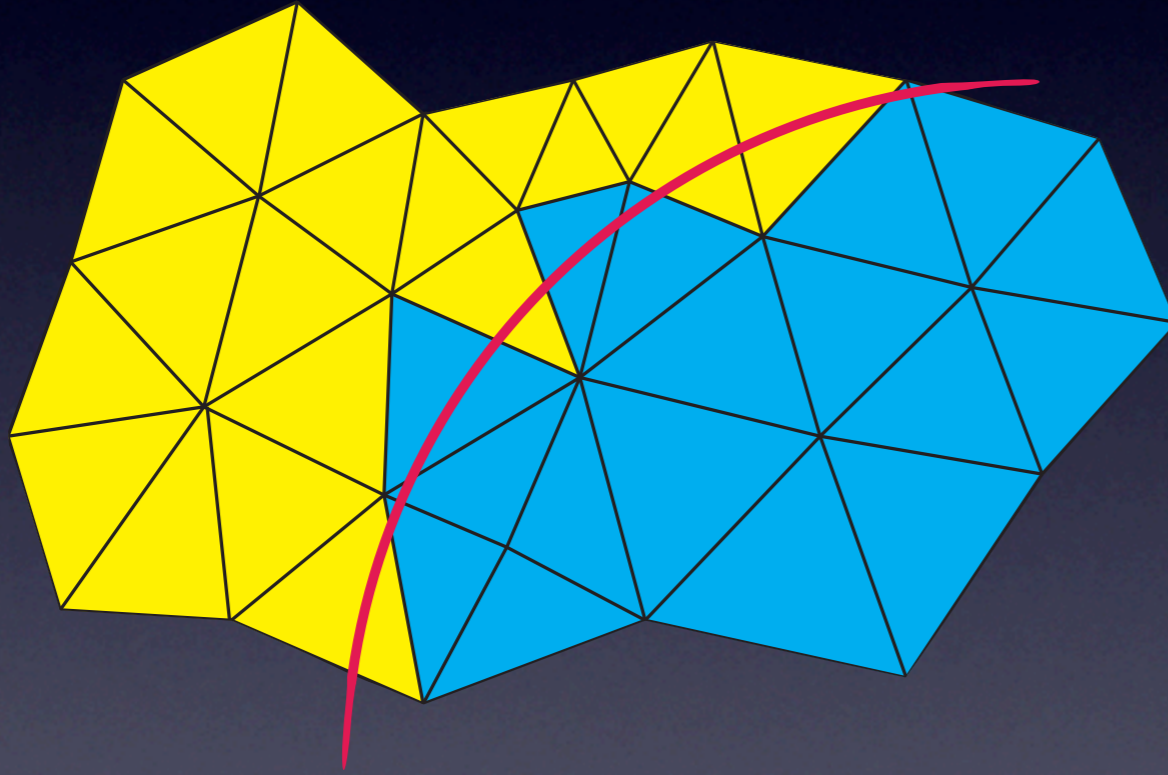


Meshing in Biology

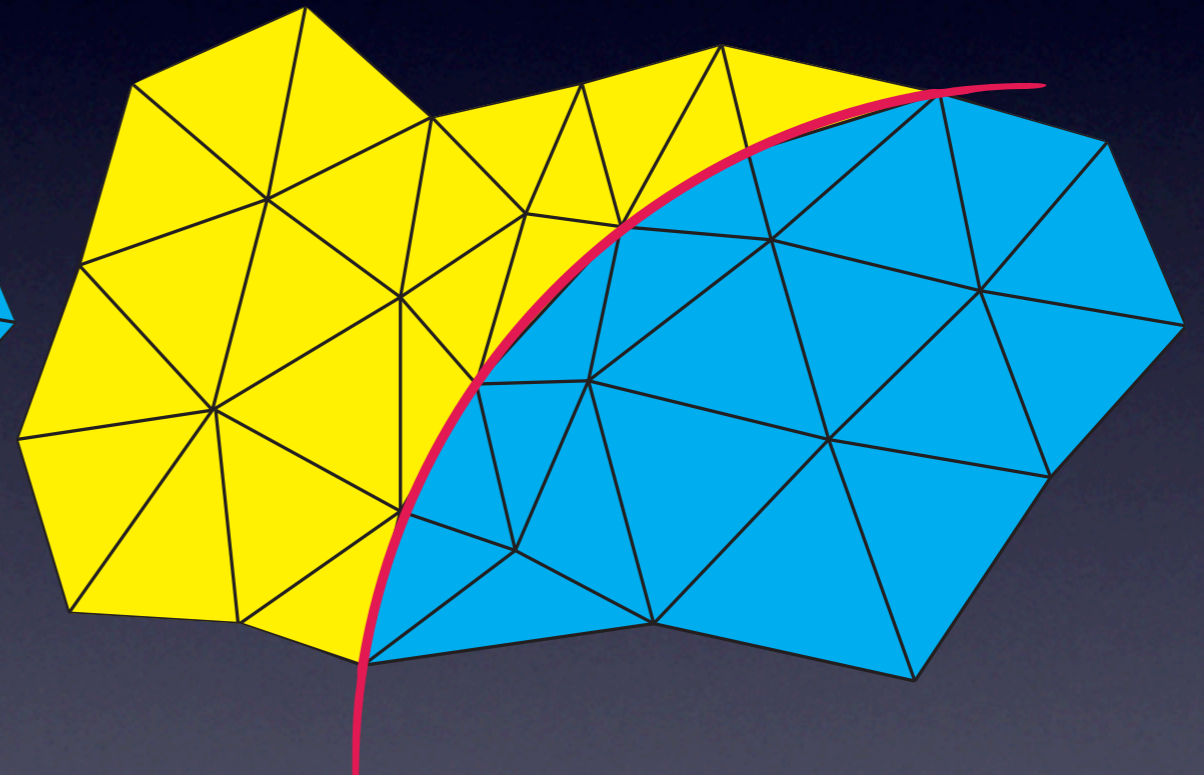


Conformal Meshing

Non-Conformal
Mesh

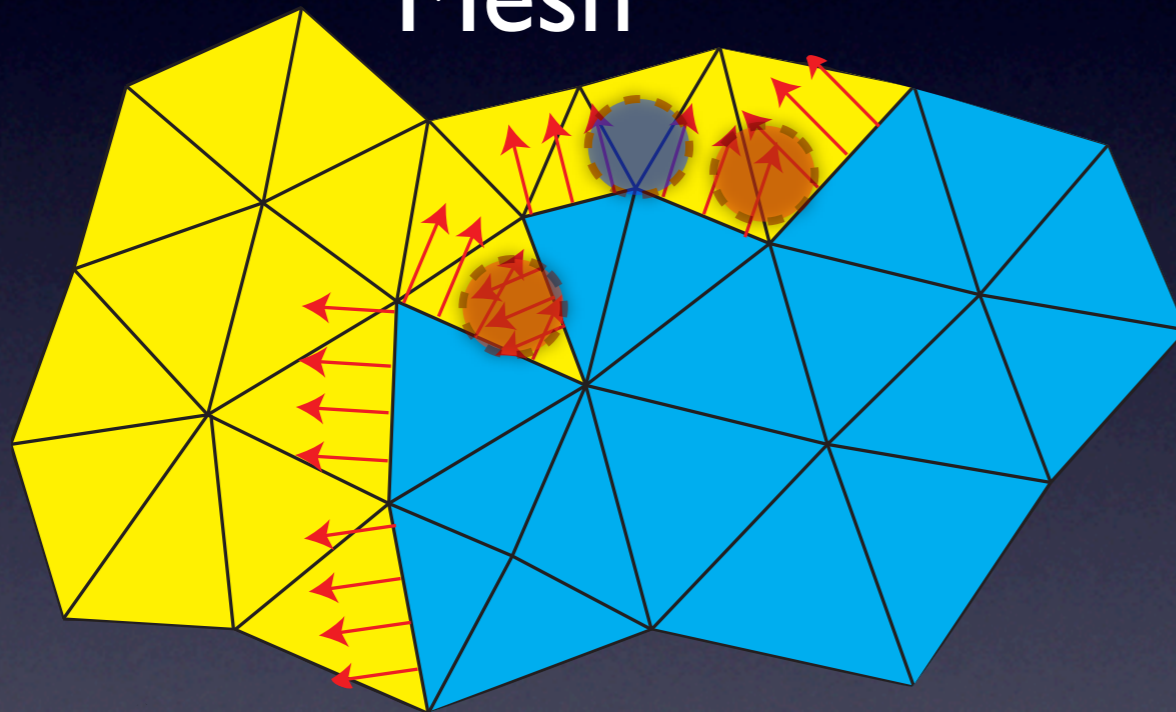


Conformal Mesh

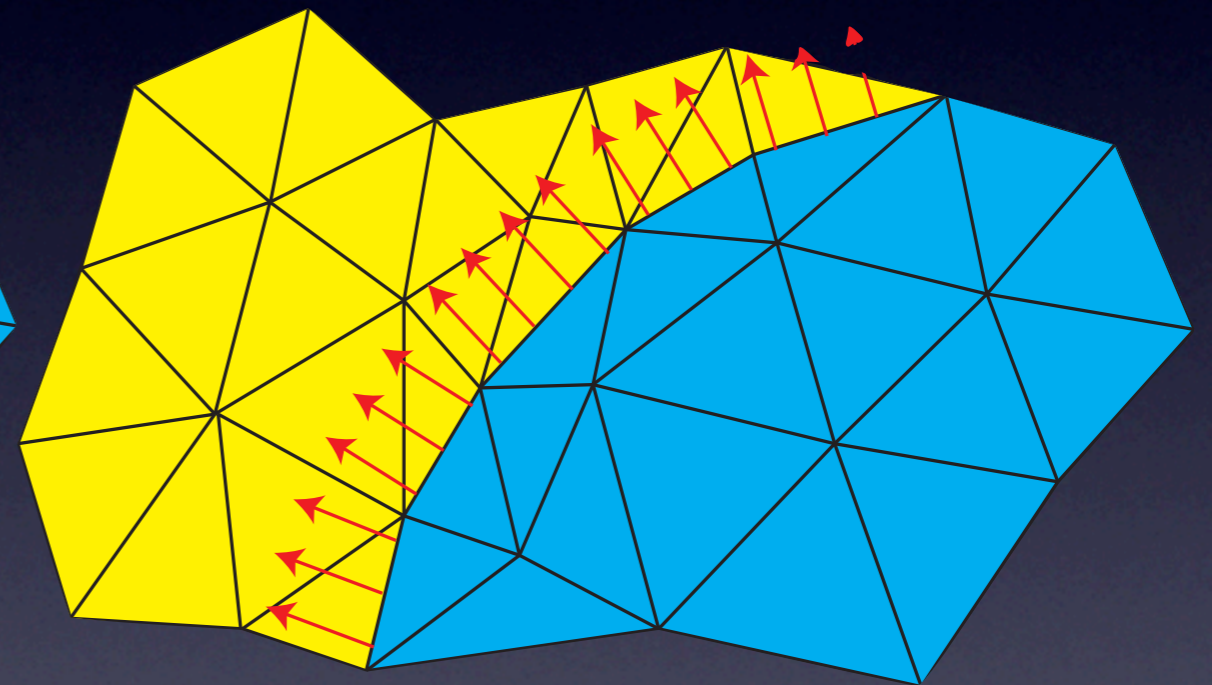


Conformal Meshes better?

Non-Conformal
Mesh

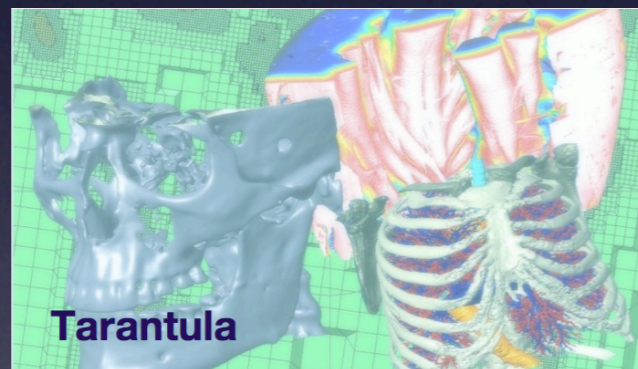
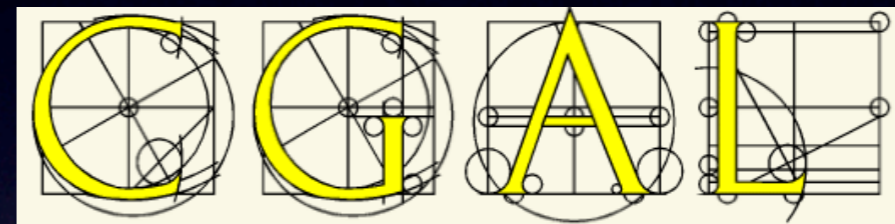
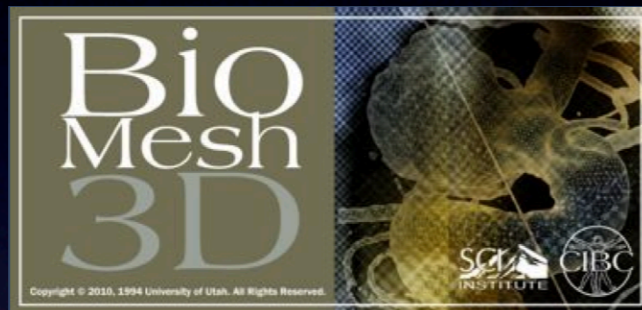


Conformal Mesh



Still an open question!

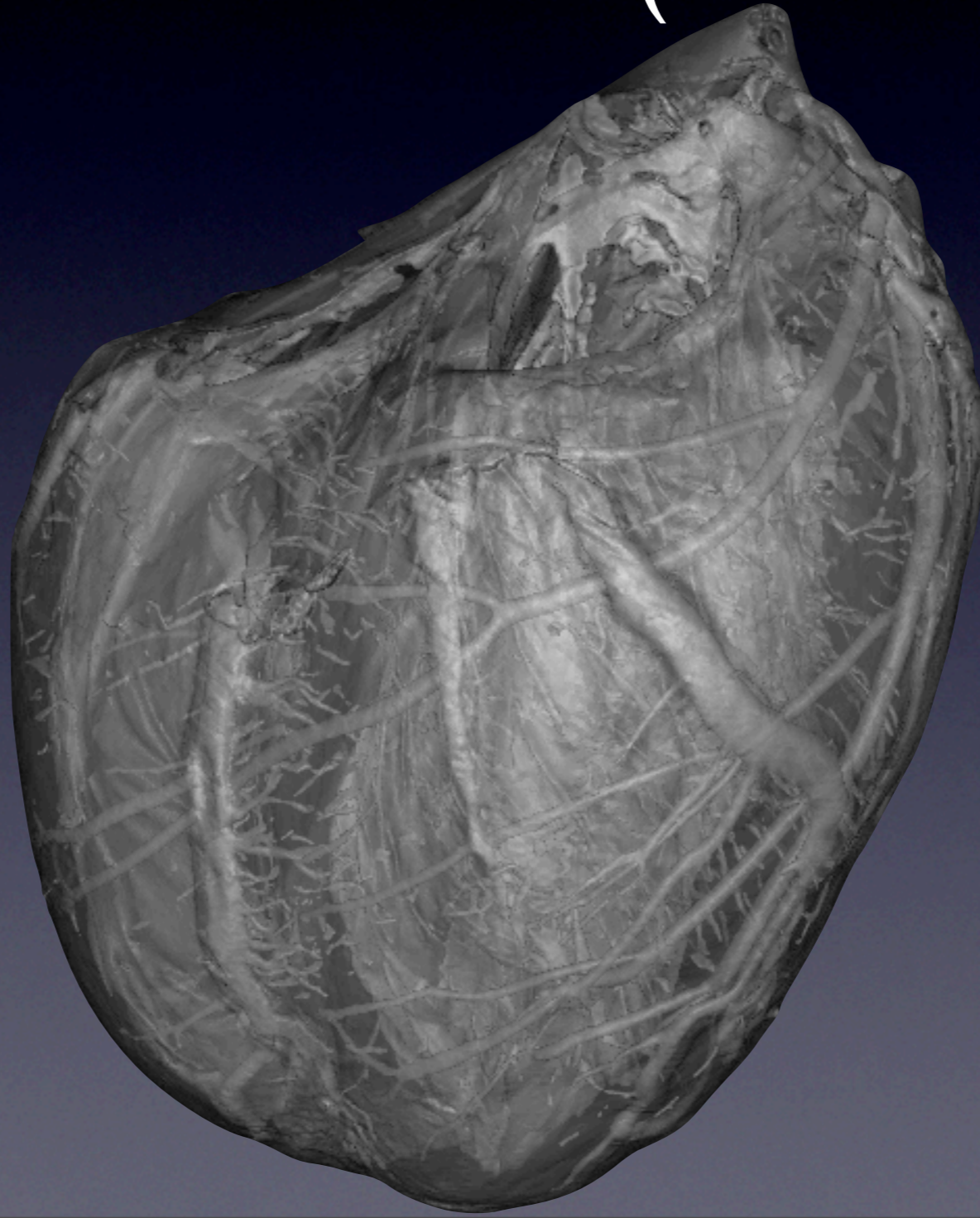
Meshing packages



and many more ...

Example - Heart

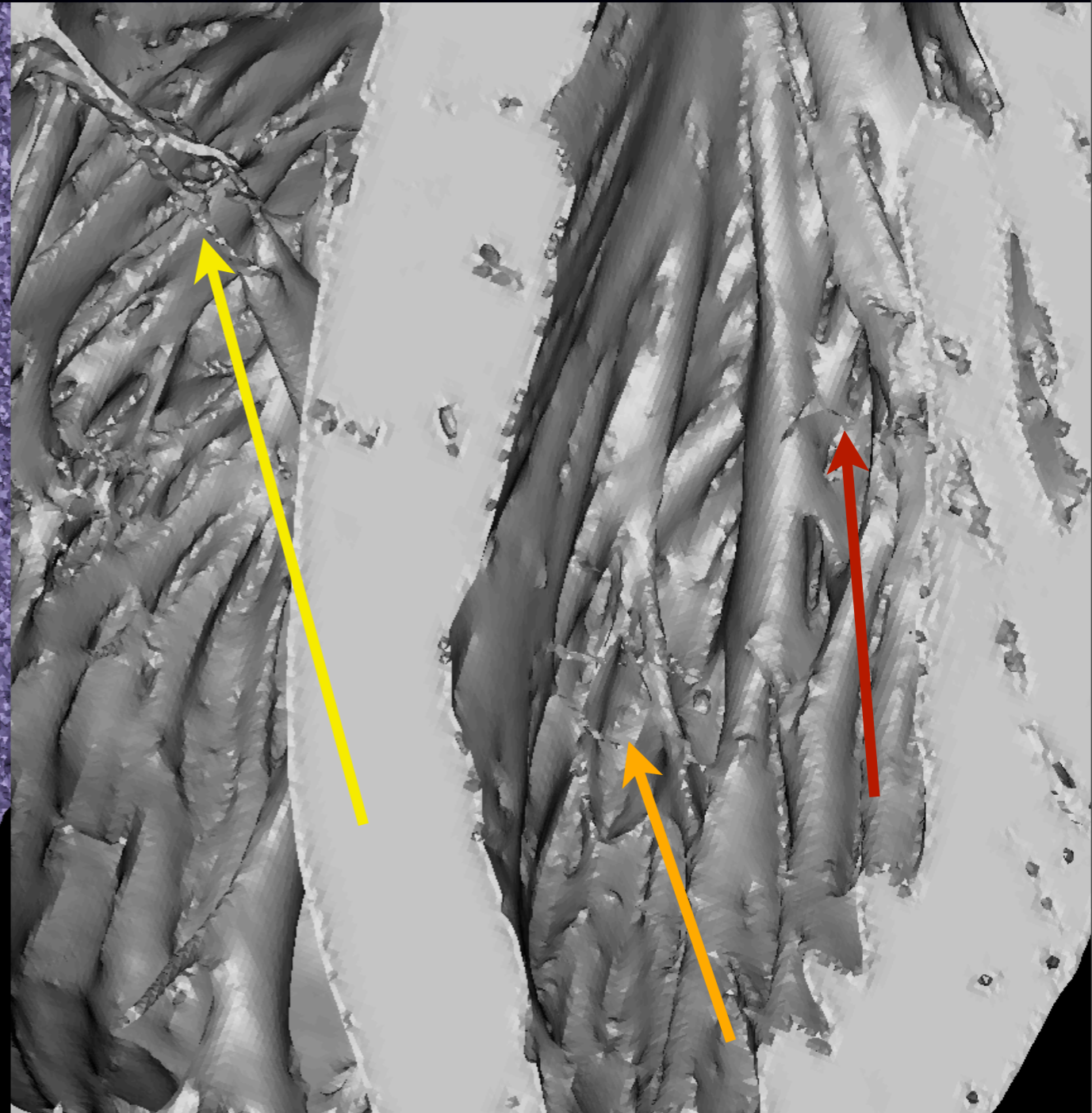
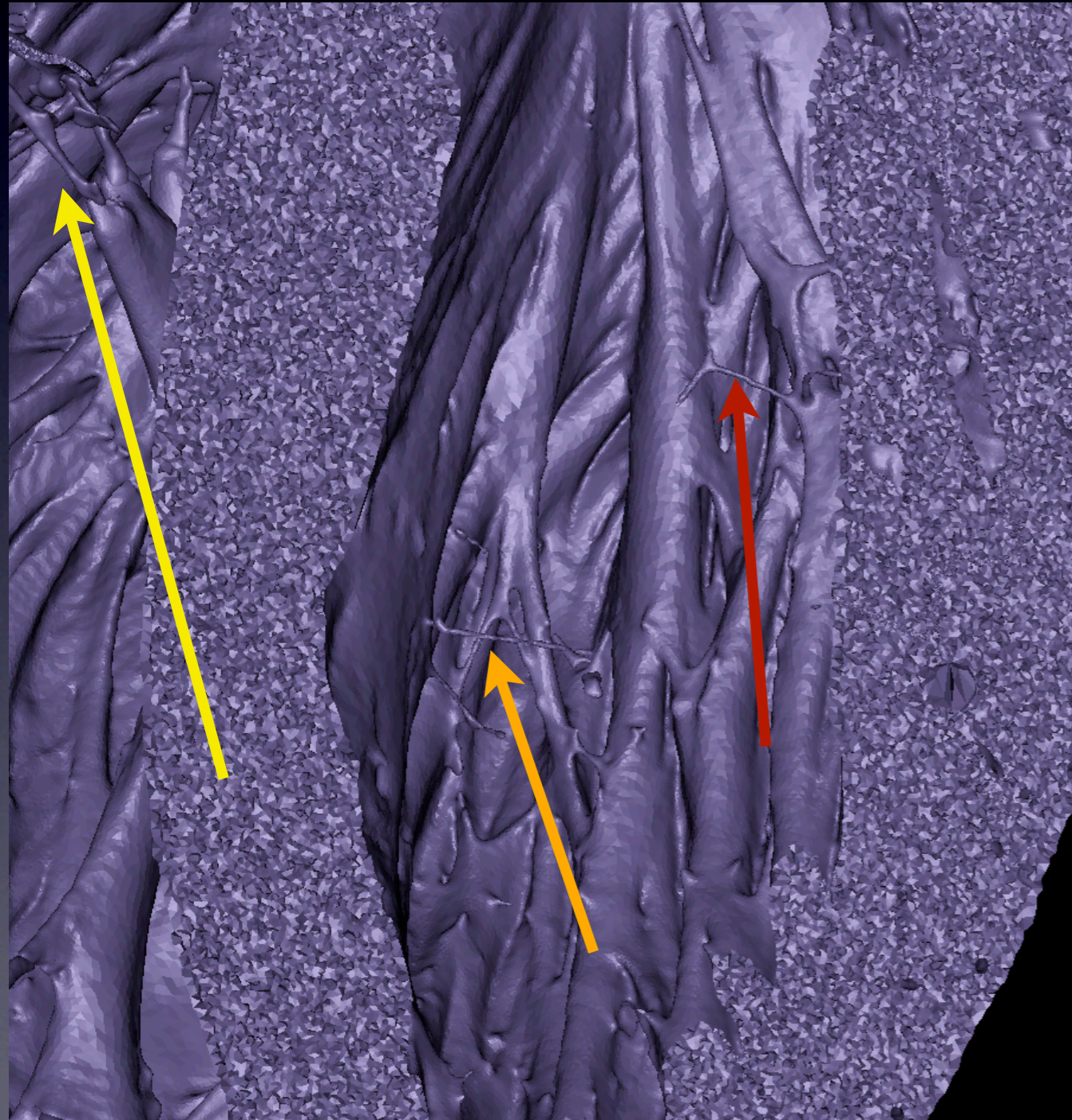
- Oxford Rabbit Heart (BioMesh3D)



Cross Section of Heart

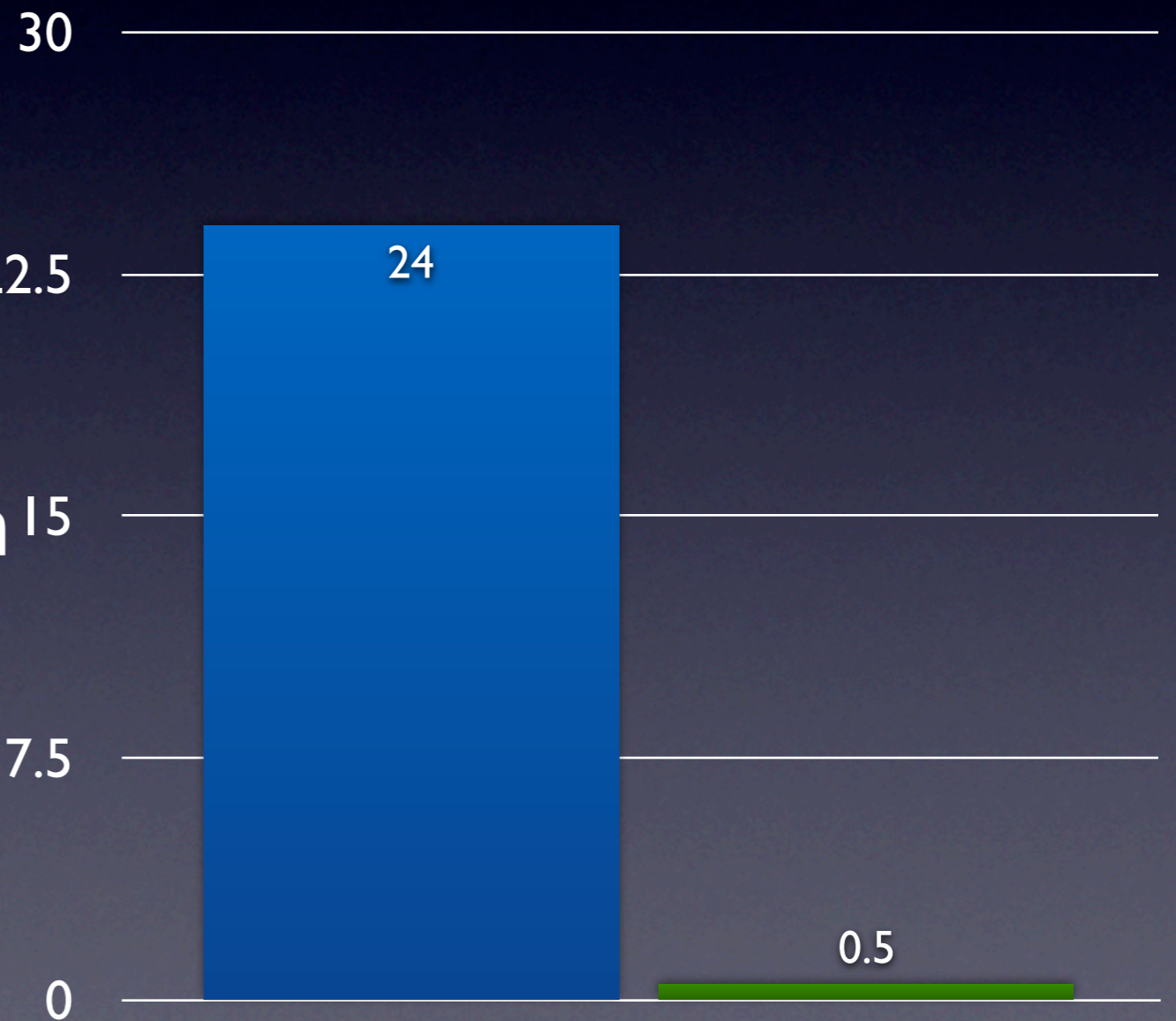
BioMesh3D

Tarantula



Comparison - Run Time

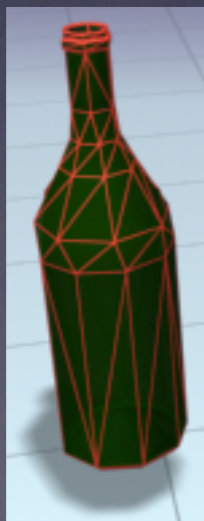
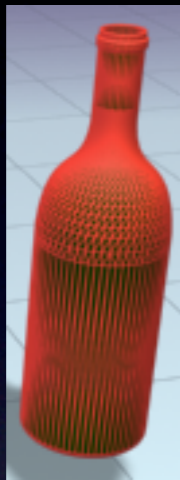
■ BioMesh3D ■ Tarantula



Time in ¹⁵
[hours]

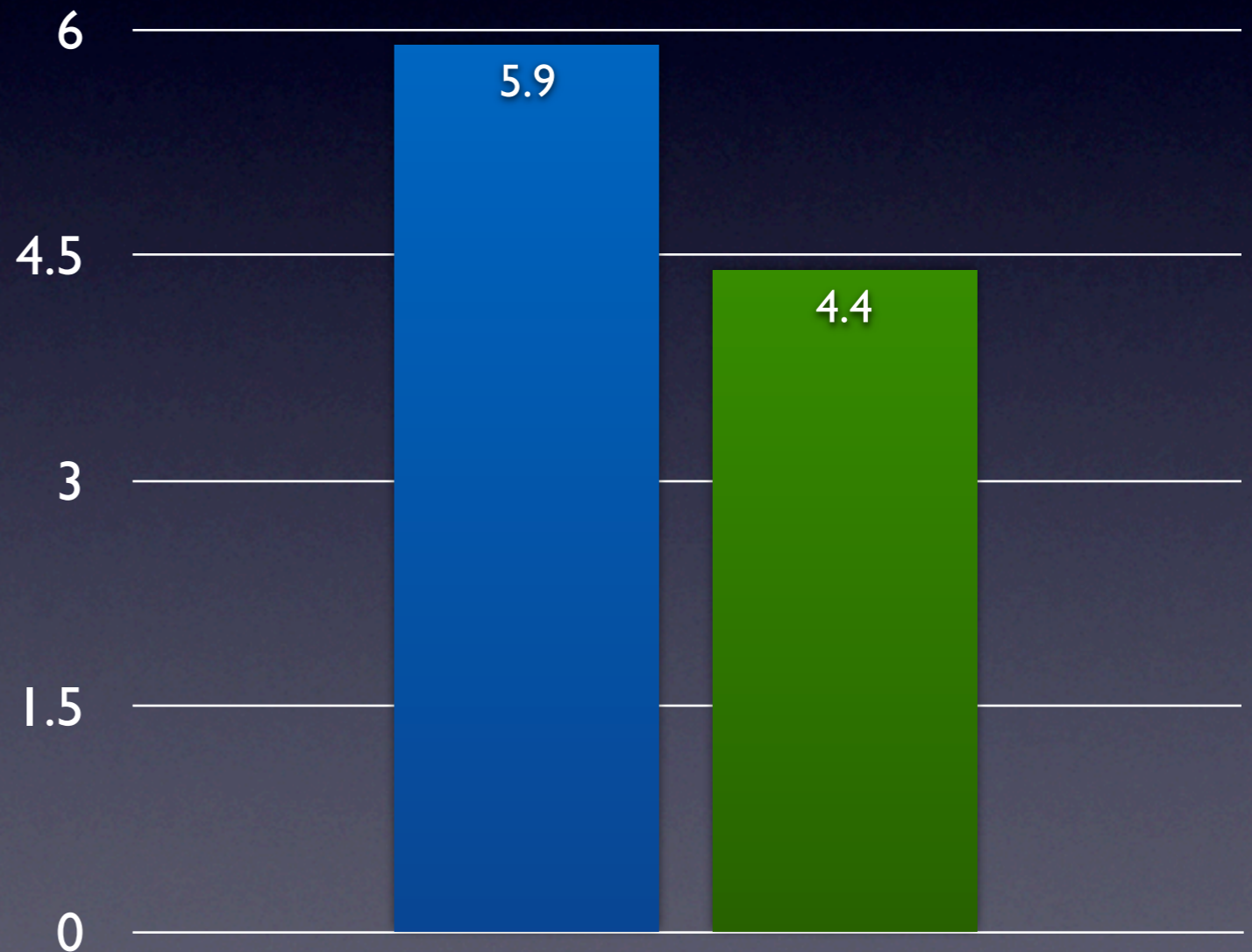


Comparison - Complexity



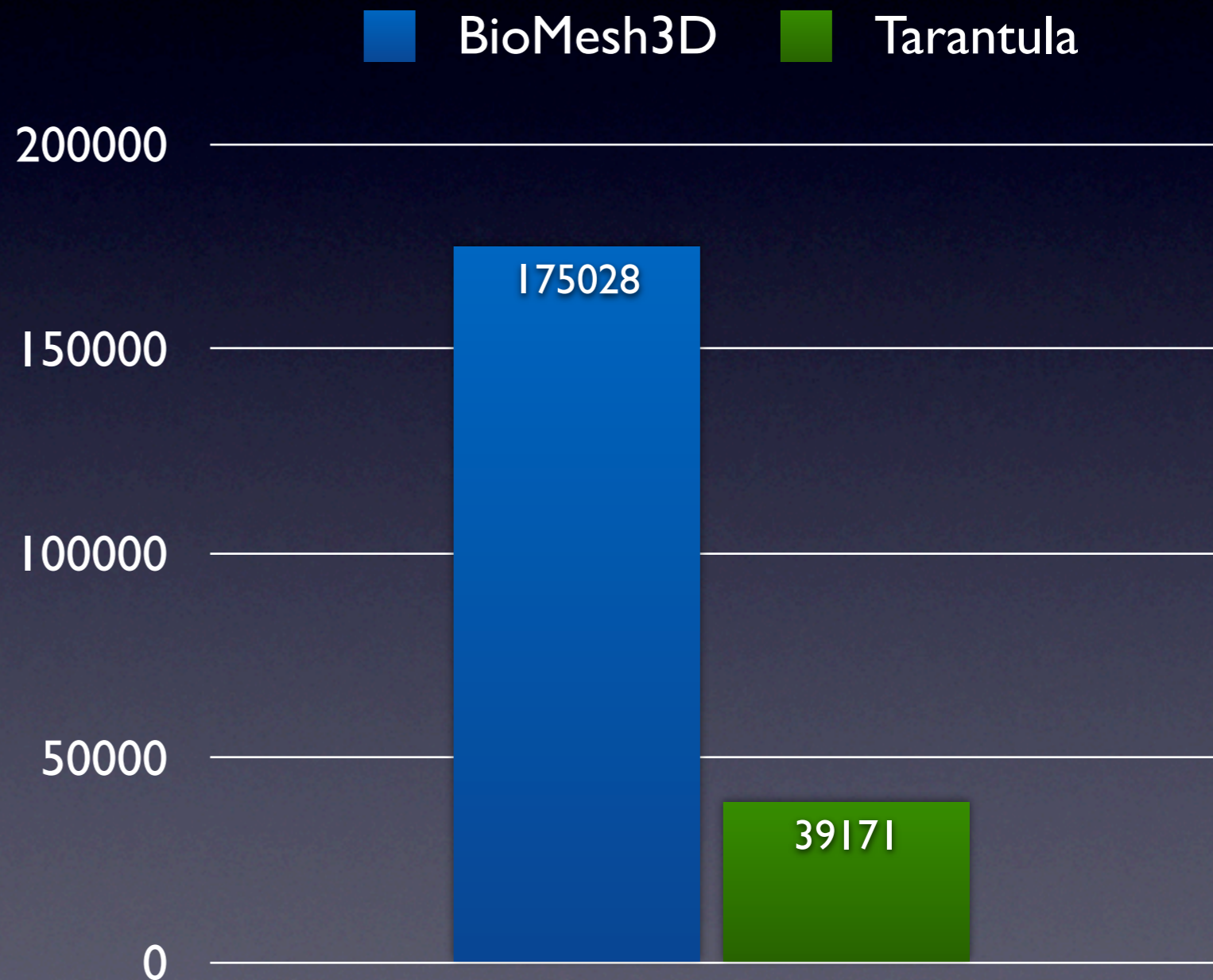
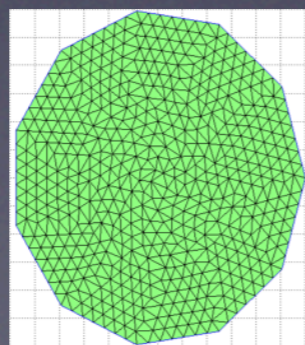
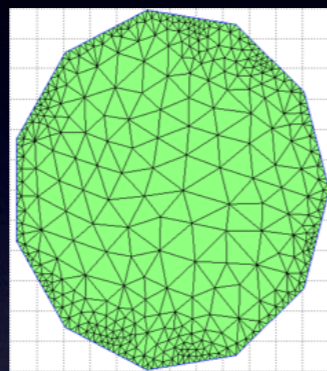
Mesh
nodes in
[xMillion]

■ BioMesh3D ■ Tarantula



Comparison - Adaptivity

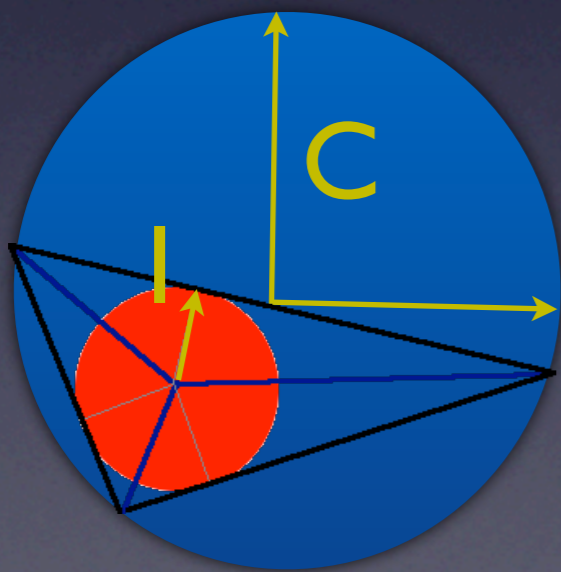
Size variability
of FE -
Stddev. of
Volumes in
[μM^3]



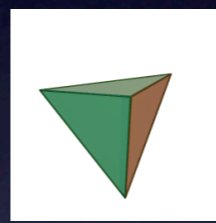
Comparison - Element Quality

scaled inscribed (I) to
circumscribed ratio (C)
(SICR)

$$\text{SICR} = 3 * I / C$$



Regular



SICR

Flat

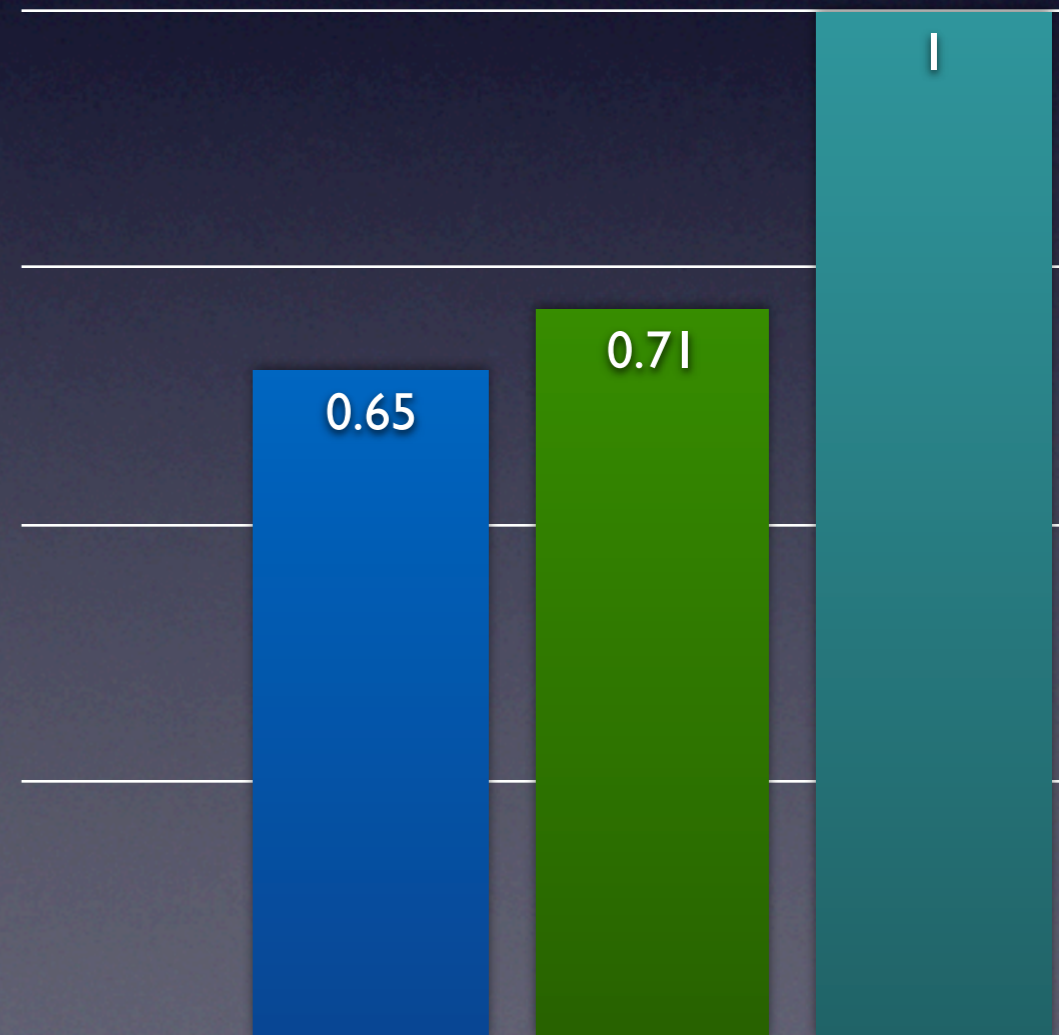
0.75

0.5

0.25

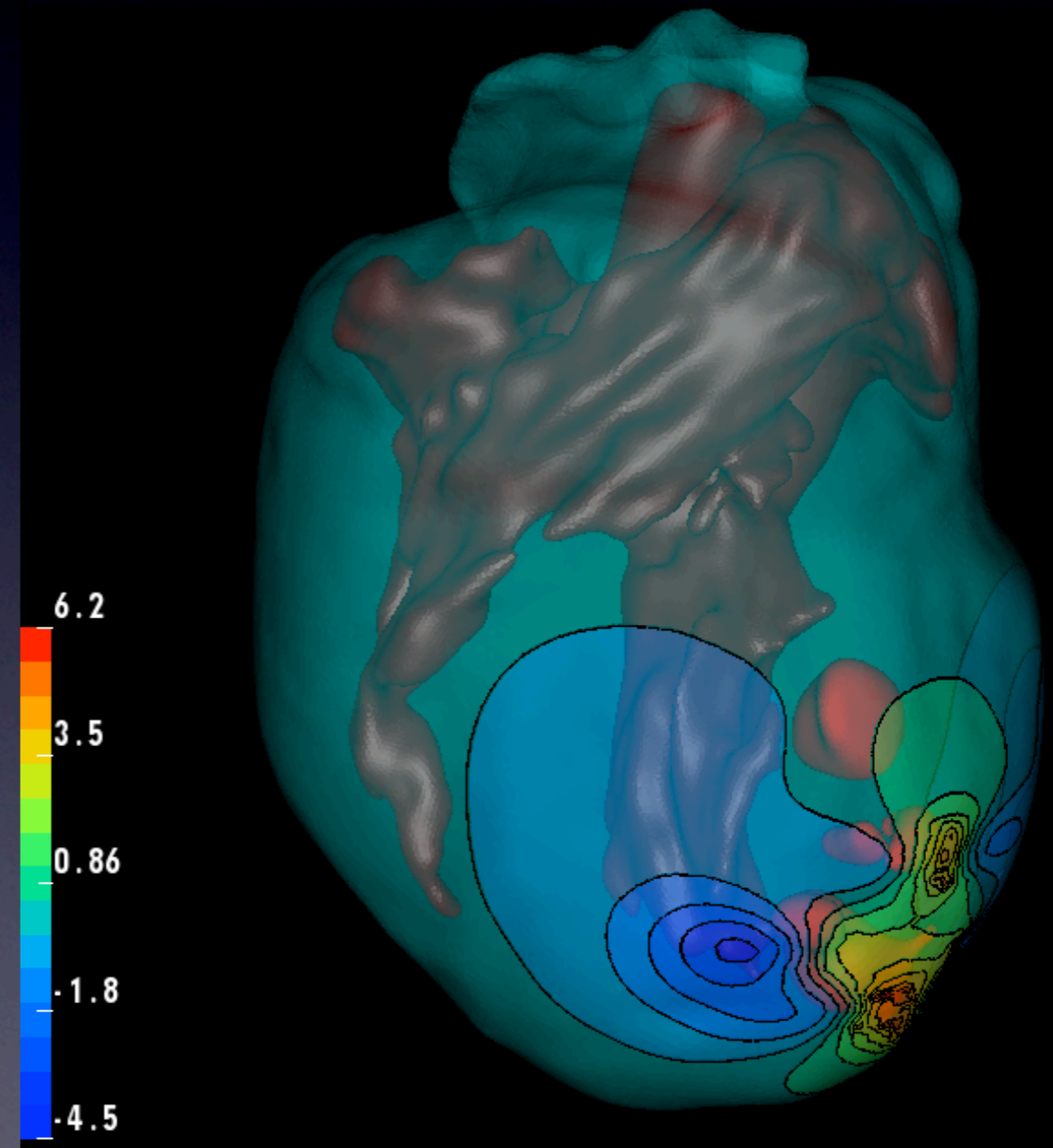
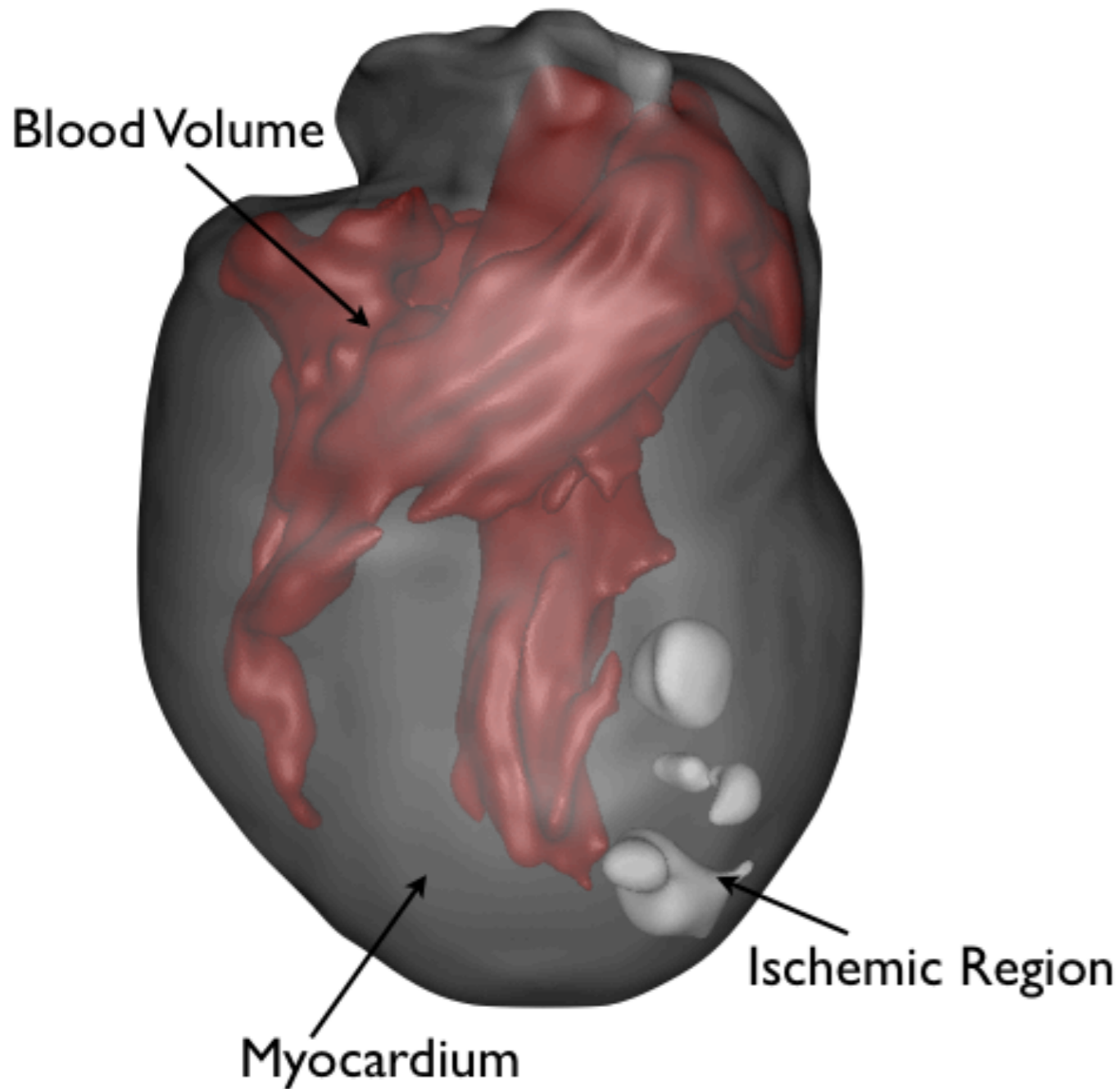
0

- BioMesh3D
- Tarantula
- optimal Elements



BioMesh3D-Pros/Cons

Single Time Point



- Pro: Local refinement

- Con: Reaction/Diffusion

BioMesh3D - Properties



Pros:

- + Conforming
- + Highly Adaptive
- + Preserve smooth/
small features



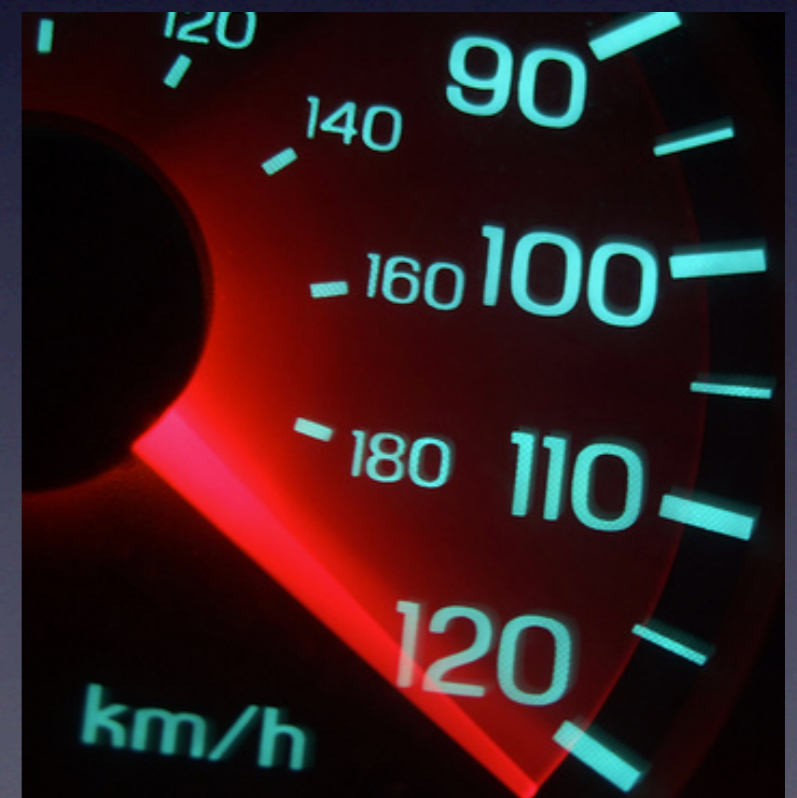
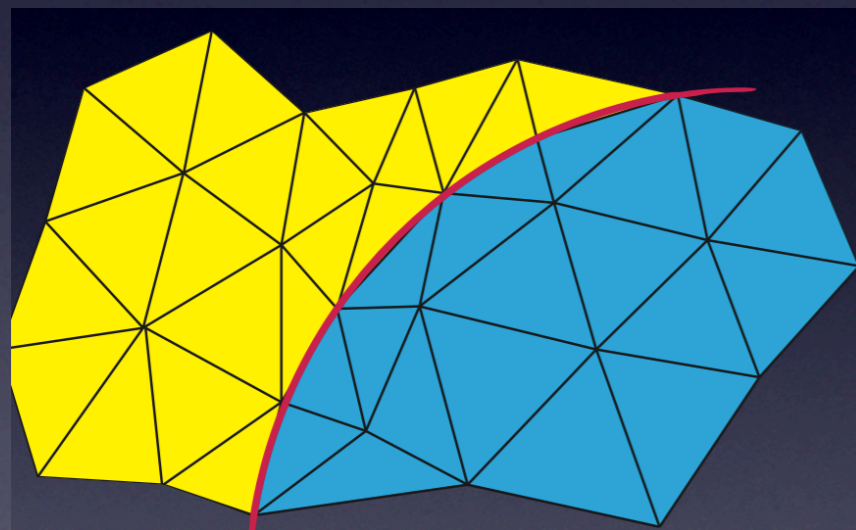
Cons:

- Robustness
- Usability
- Run time
- Sufficient node density
- Element Quality

New meshing Approach: “Clever”



$$\min(\text{SIQR}) \geq \text{const}$$



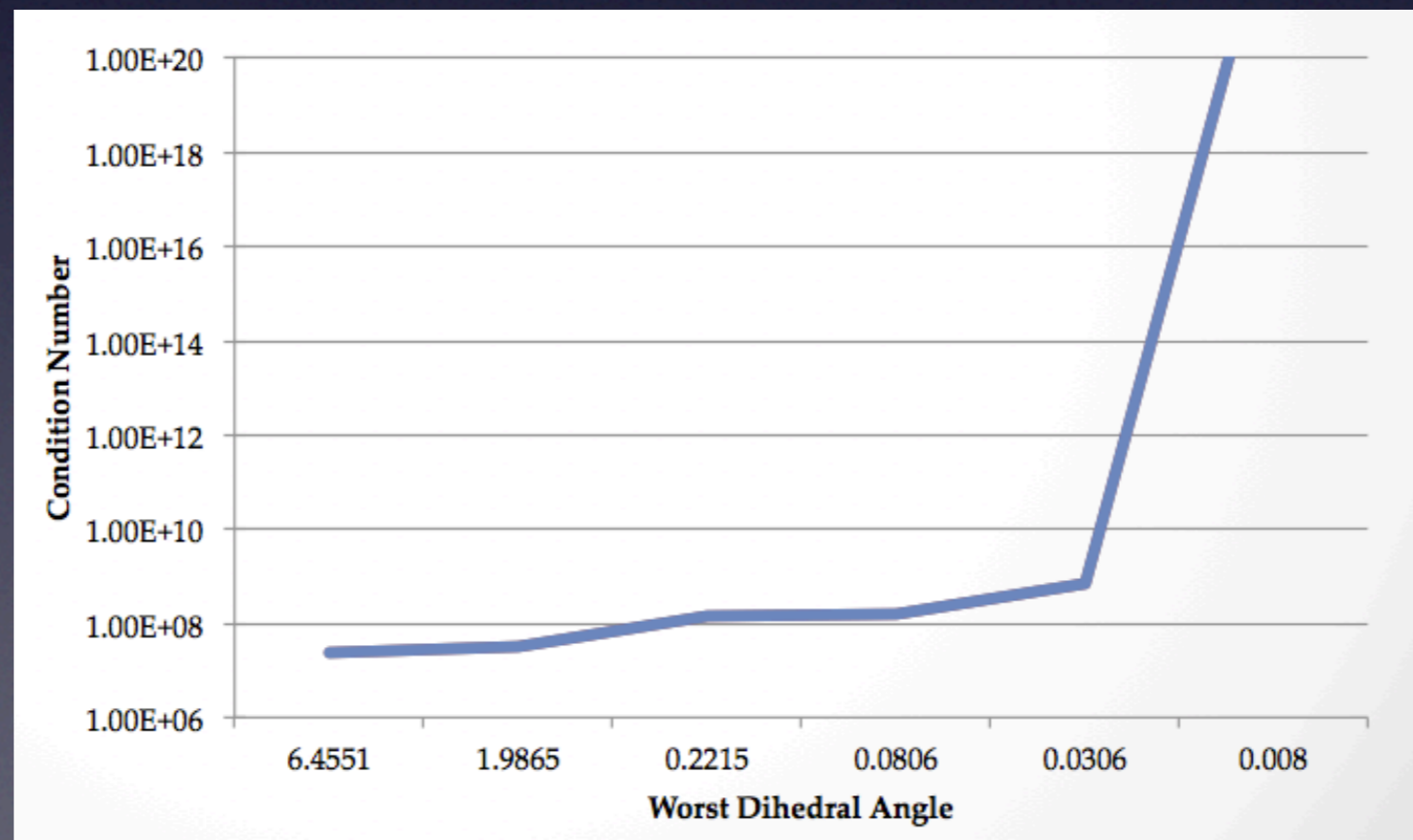
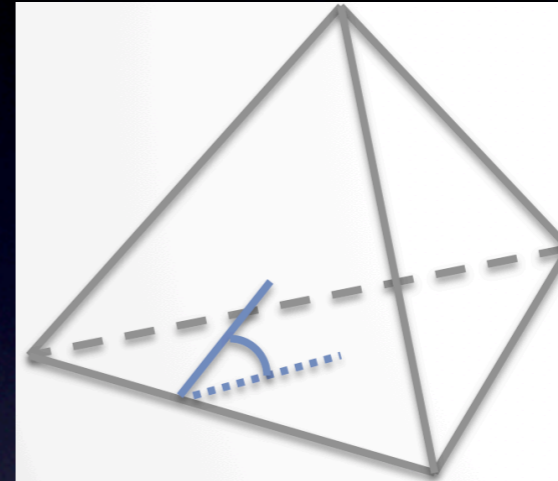
"Lattice Cleaving: Conforming Tetrahedral Meshes of Multimaterial Domains with Bounded Quality"

Bronson, J., Levine, J., and Whitaker, R.

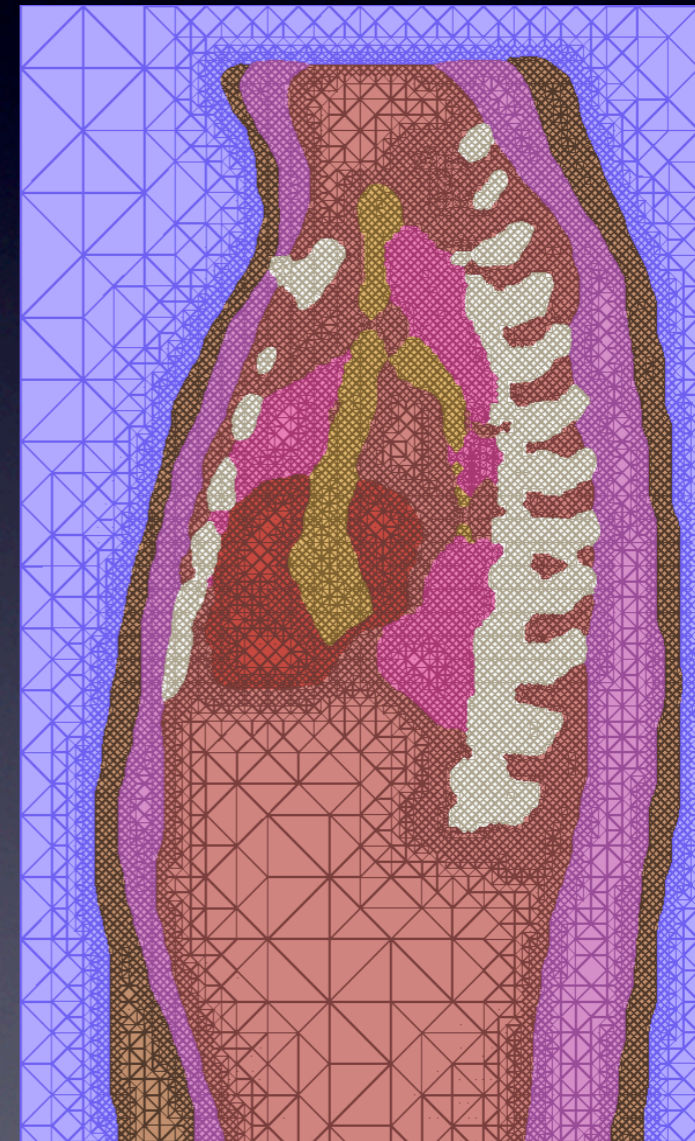
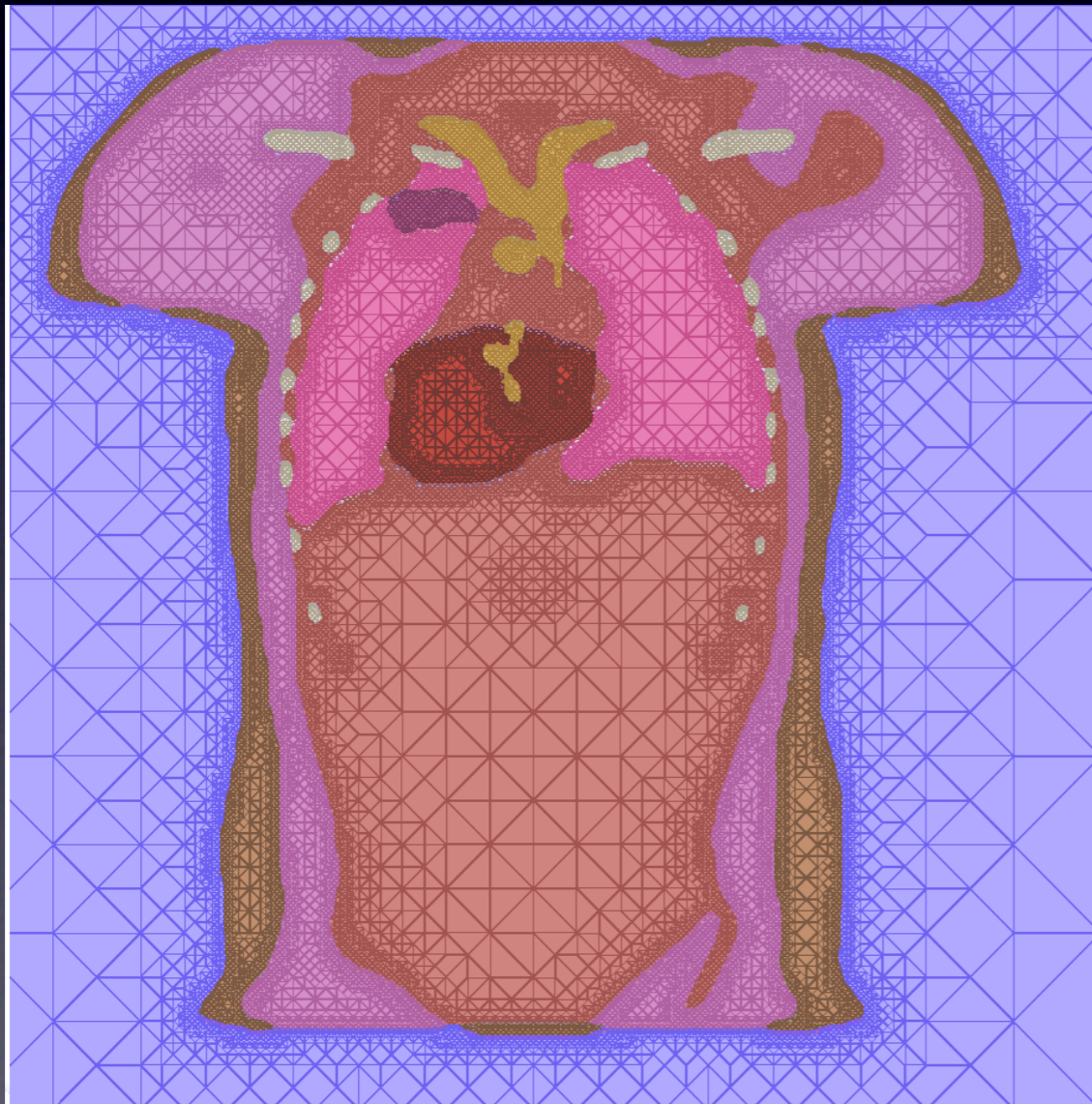
To appear in Proceedings of the 21st International Meshing Roundtable (San Jose, CA, Oct 7 - 10, 2012)

Element quality

- Dihedral Angle
- Condition number



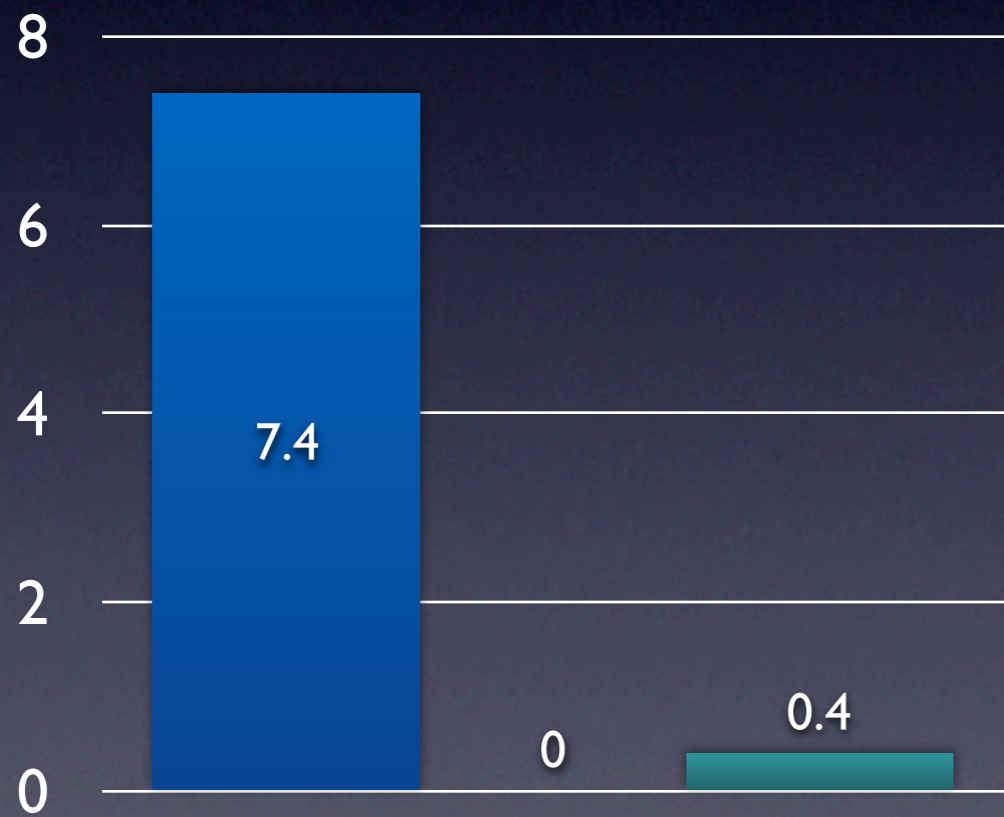
Comparison - Torso



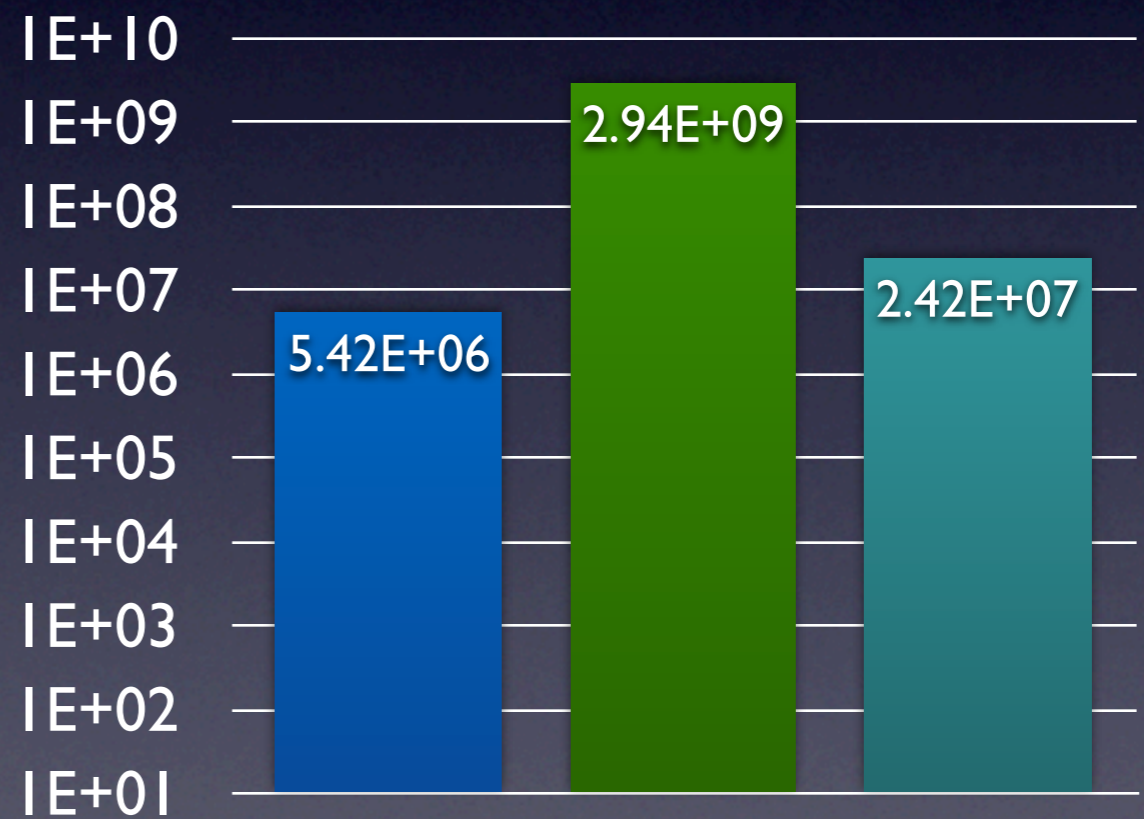
Cleaver Mesh Result

Comparison - Torso

Cleaver BioMesh3D CGAL

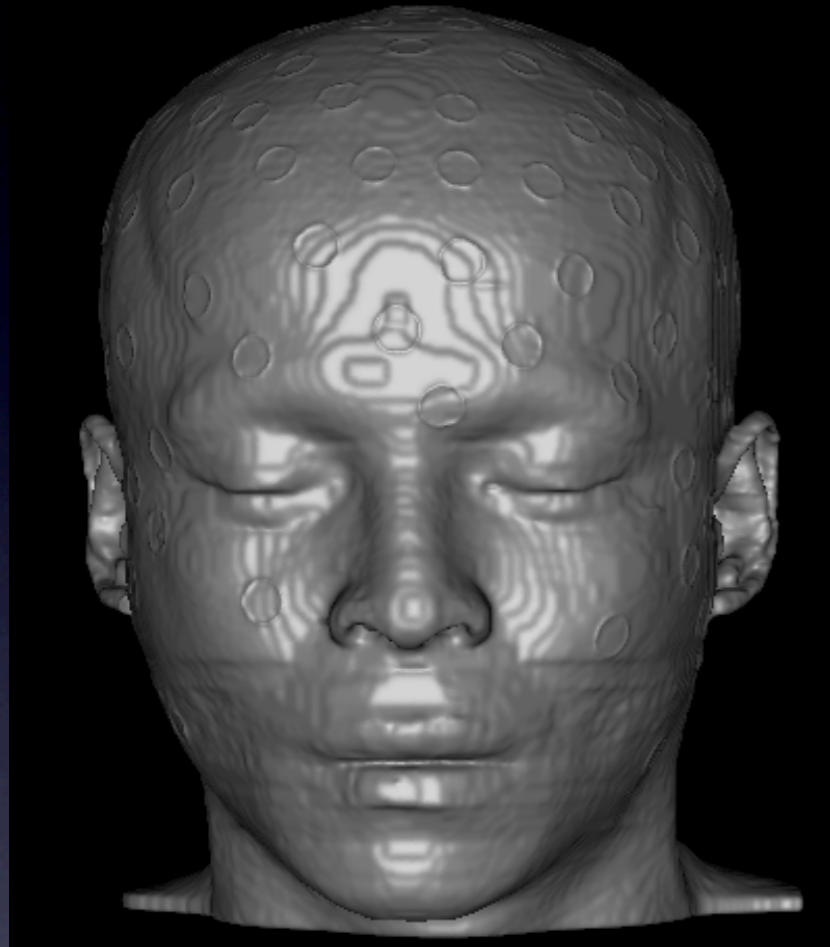


min(Dihedral Angle)

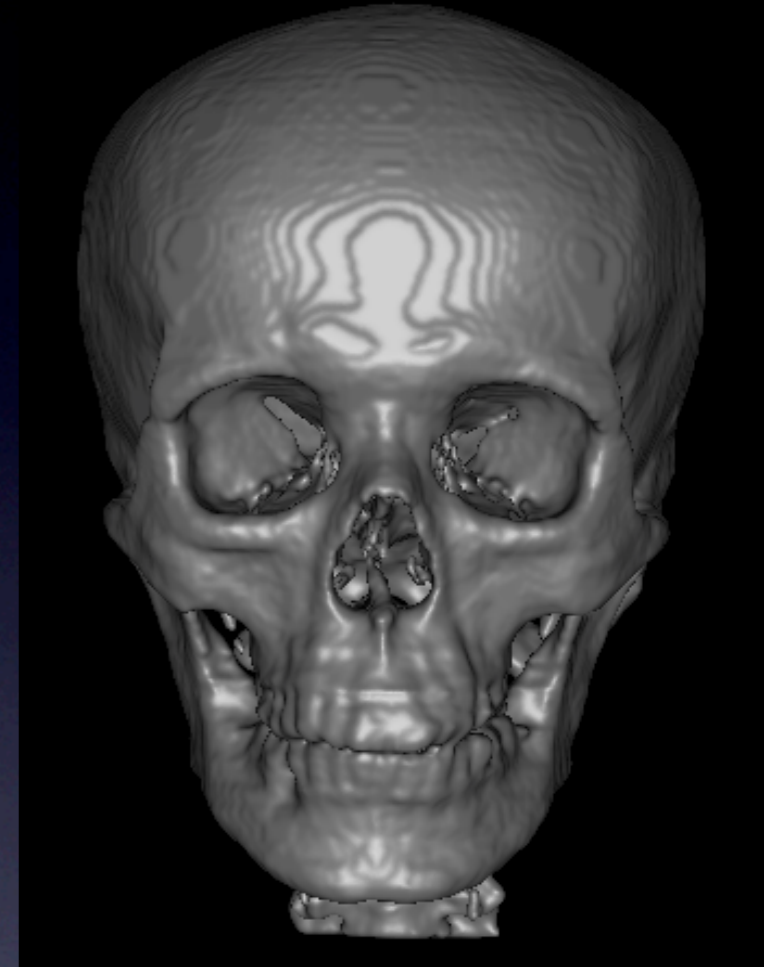
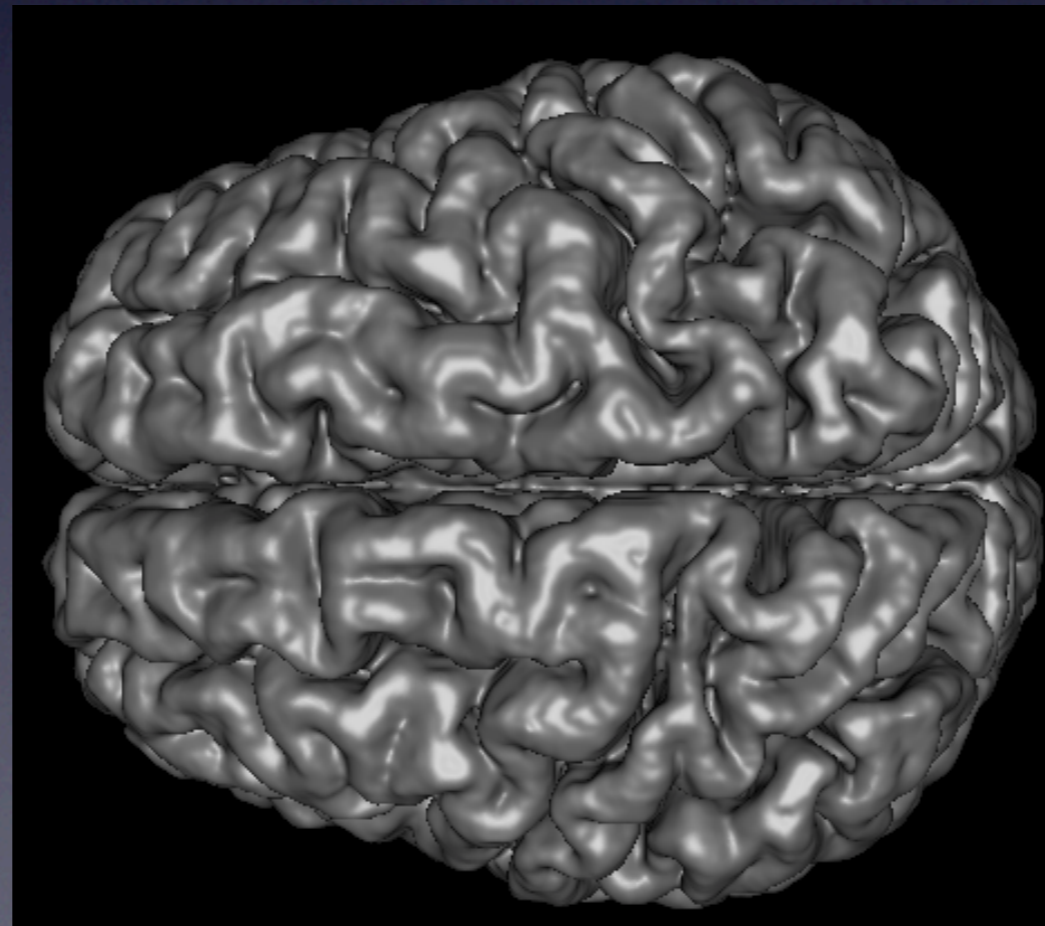


Condition number

Comparison - Head



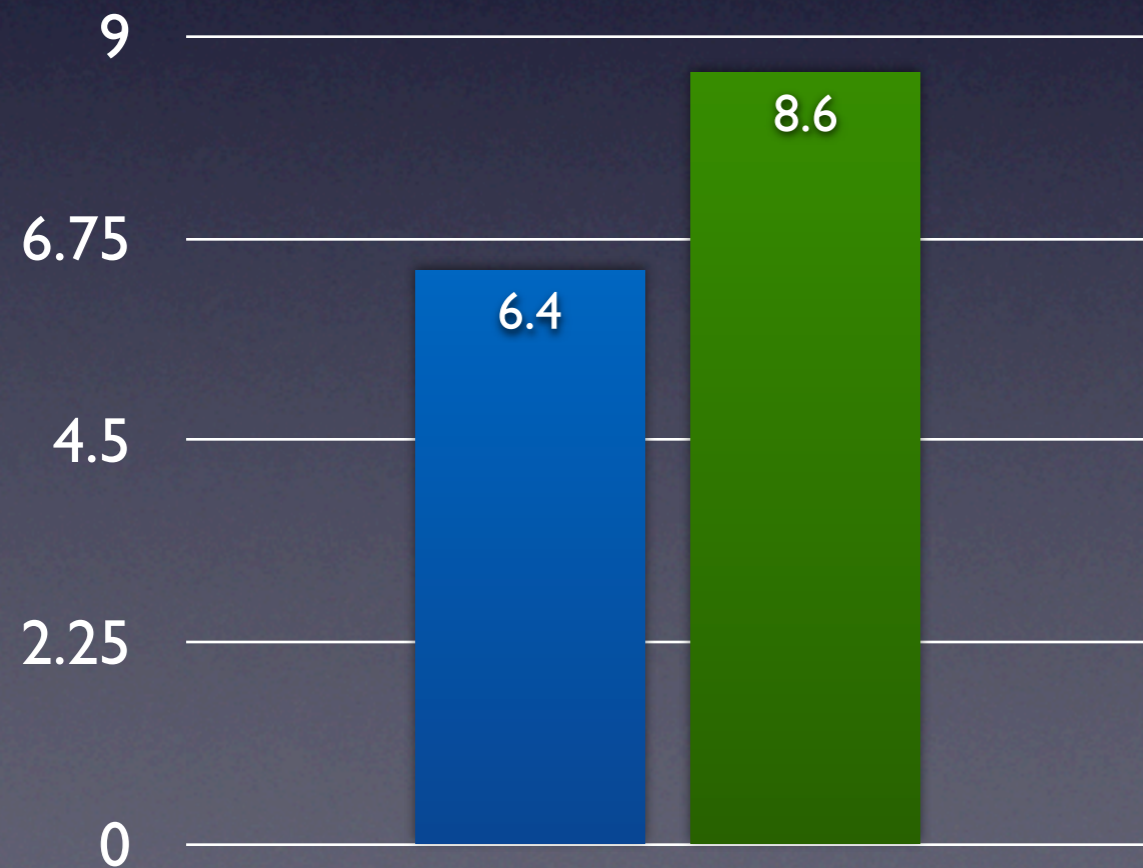
8 Materials



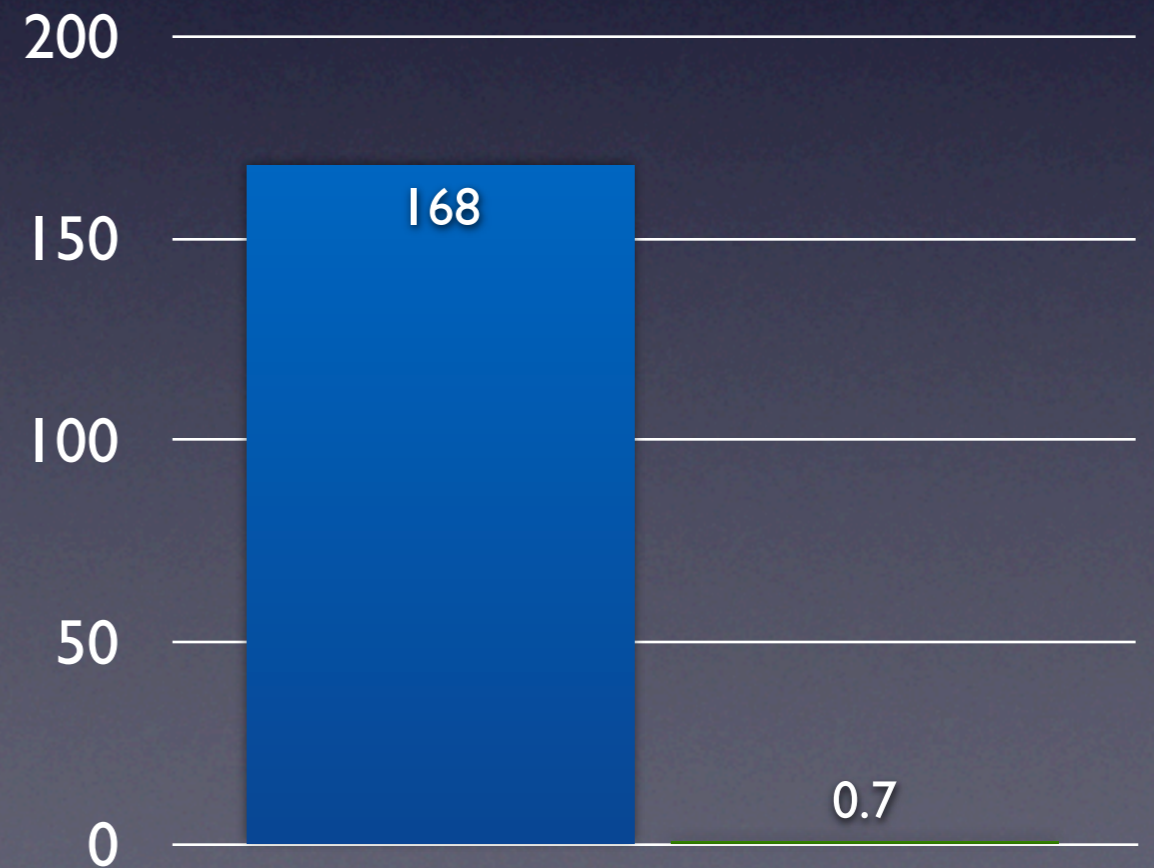
Comparison - Head

■ BioMesh3D ■ Cleaver

Mesh
nodes in
[xMillion]

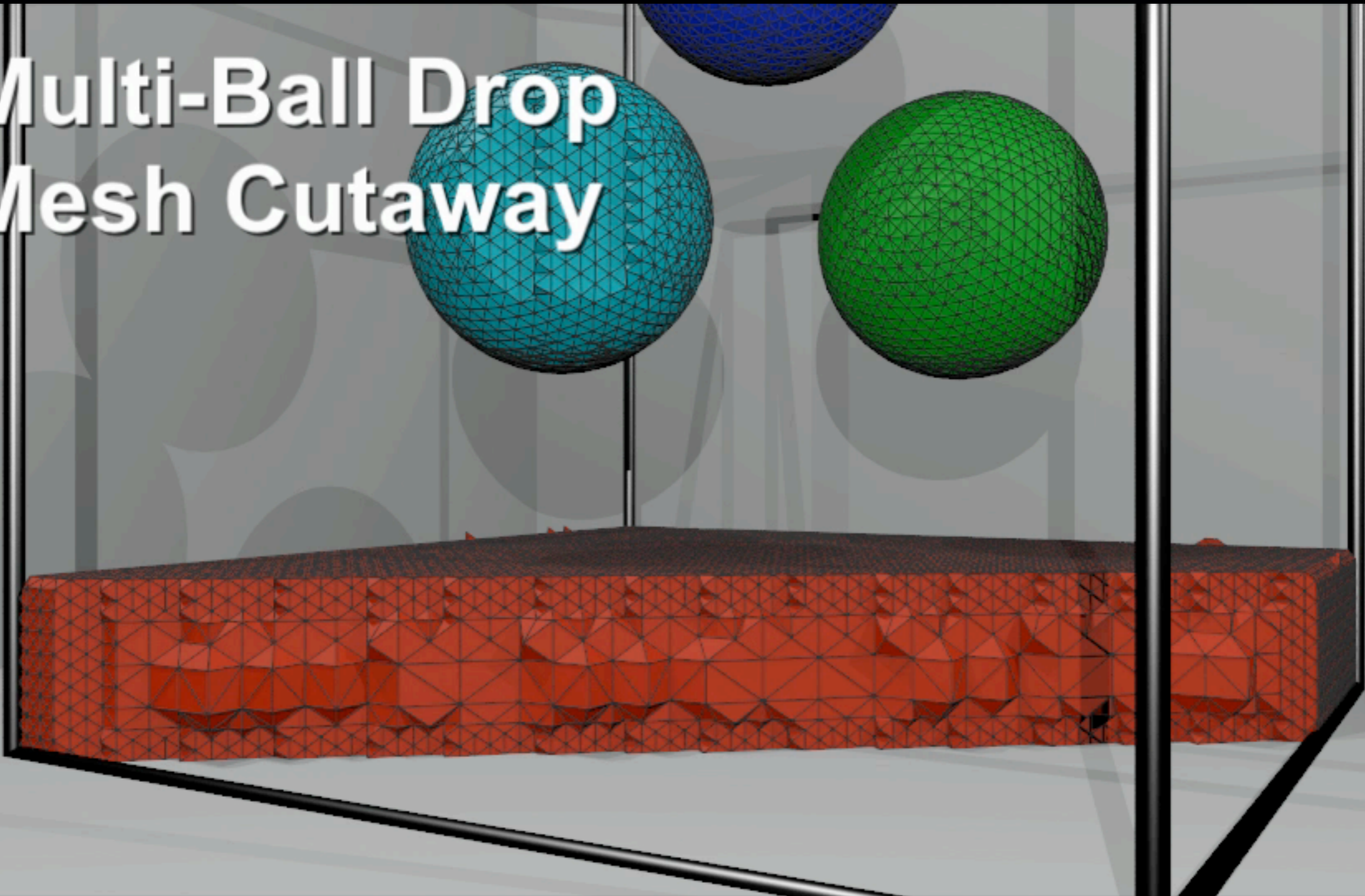


Time in
[hours]



Cleaver in Action

Multi-Ball Drop
Mesh Cutaway



Cleaver

- First Release: Fall 2012
- Features:
 - Incredibly fast
 - Conforming
 - Guarantees on Quality
 - Input support: SCIRun - NRRD
 - Output supports:
 - SCIRun pts/elems
 - TetGen node/elems
 - MATLAB Binaries